

An Iterative Learning Control Approach for Radio Frequency Pulse Compressor Amplitude and Phase Modulation

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Paper available at: <http://control.ee.ethz.ch/index.cgi?page=publications&action=details&id=5288>

Pulse compression to achieve higher accelerating gradients

- AKA “SLED” - SLAC Linac Energy Doubler
- Idea: Take the relatively long RF pulse generated by a klystron (around $3 \mu\text{s}$), and compress it to achieve a higher amplitude pulse over a shorter time (around $0.7 \mu\text{s}$).
- How? Feed the klystron pulse into an RF cavity, then find some way to extract the energy from the cavity quickly, and deliver it to the beam.

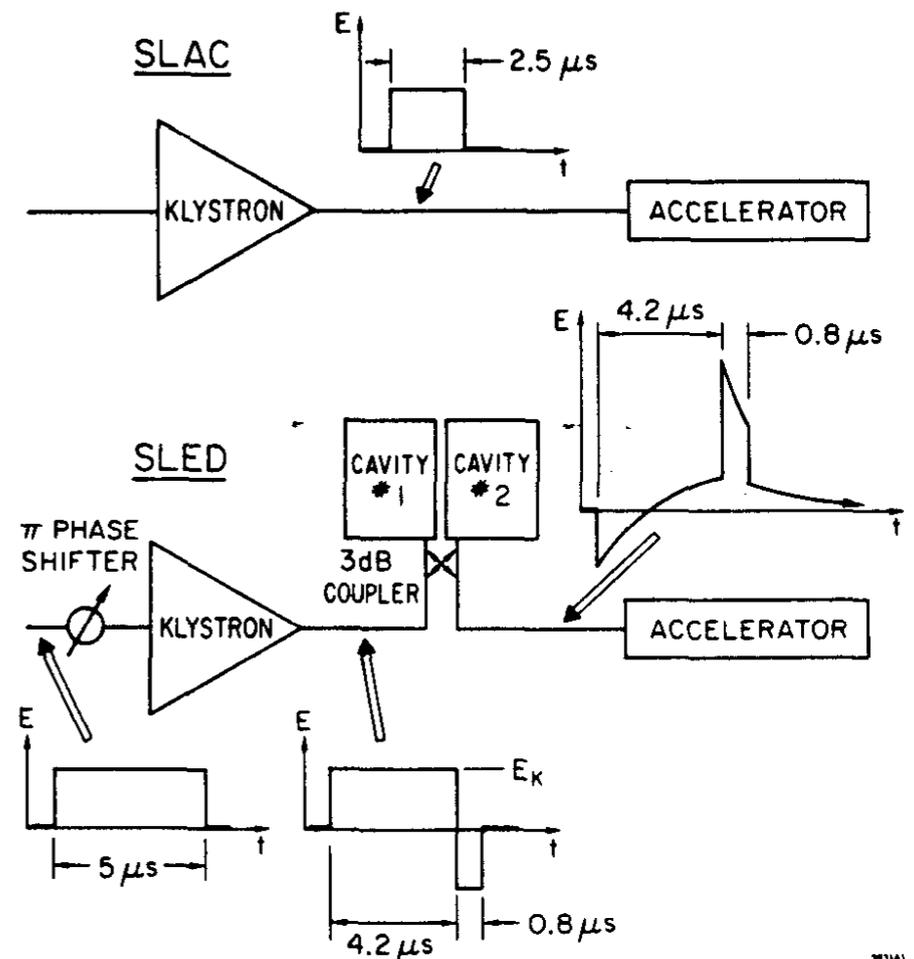


FIG. 2--A comparison of the present SLAC and SLED RF systems.

SLED: A Method of Doubling SLAC's Energy,
Z. D. Farkas, H. A. Hogg, G. A. Loew, P. B. Wilson.
1974

Great, but...

- Output amplitude has a steep slope.
- What if you want to accelerate two bunches with ~ 100 ns separation? They will end up with significantly different energies, which might not be what you want. For example, in an FEL, wavelength is proportional to electron bunch energy, so it must be set precisely to meet user requirements.
- Bunches with energy error aren't matched to the linac lattice, causing emittance blow-up.

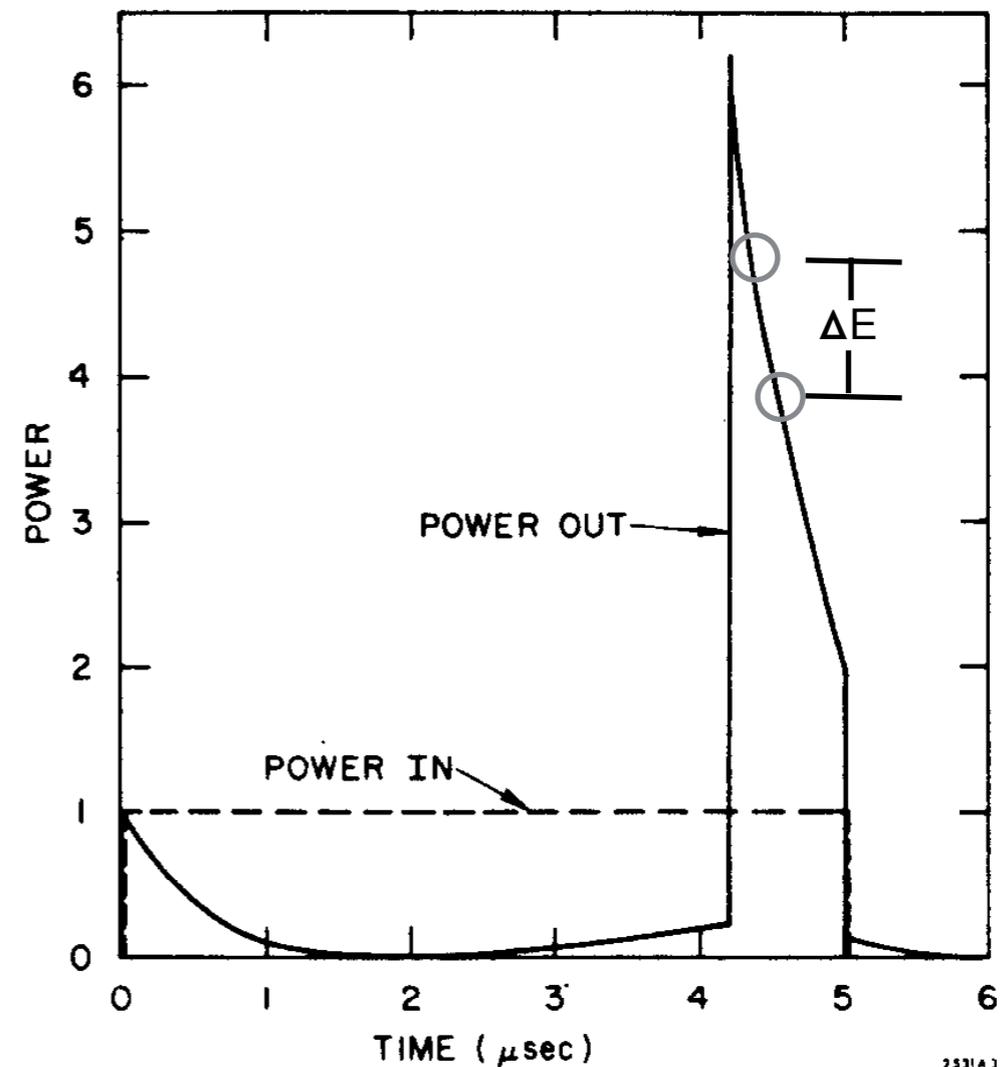


FIG. 7--Input power to and output power from the SLED microwave network as a function of time.

Controlling the output pulse shape by modulating the input to the klystron

SwissFEL's solution: build a feed-forward system that measures the output from the cavity, digitizes I and Q waveforms, then determines a correction to apply to the klystron drive pulse.

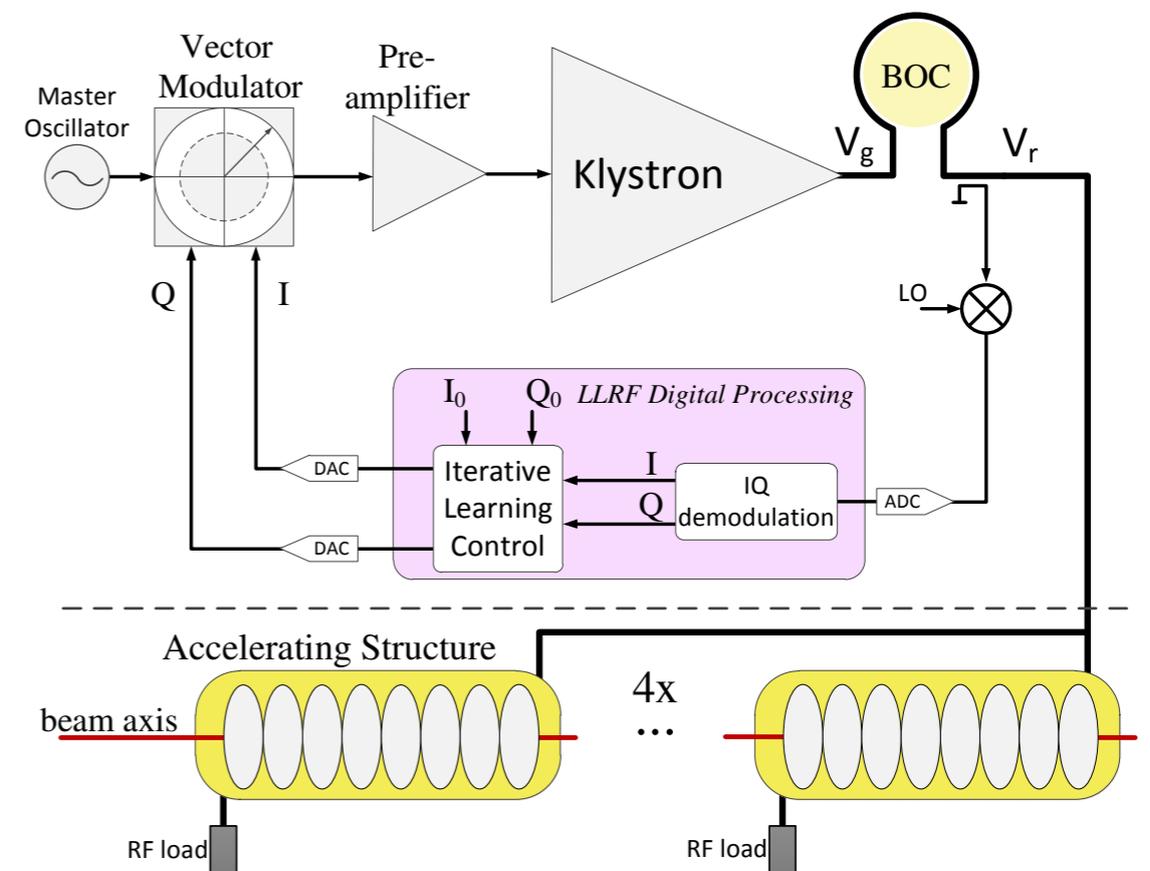


Figure 1: The simplified RF layout of a C-band RF station in the SwissFEL beamline.

Hardware setup

- Looks pretty standard: convert the cavity output to IF, digitize, and demodulate to an I and Q representation digitally.
- An “Iterative Learning Control” system calculates a function by comparing the measured I and Q to reference I and Q waveforms (they just want to make phase and amplitude constant over the output pulse duration, but could probably design a custom shape too)
- Transfer function for RF amplifier chain + cavity is used to calculate new I and Q waveforms for klystron drive pulse.

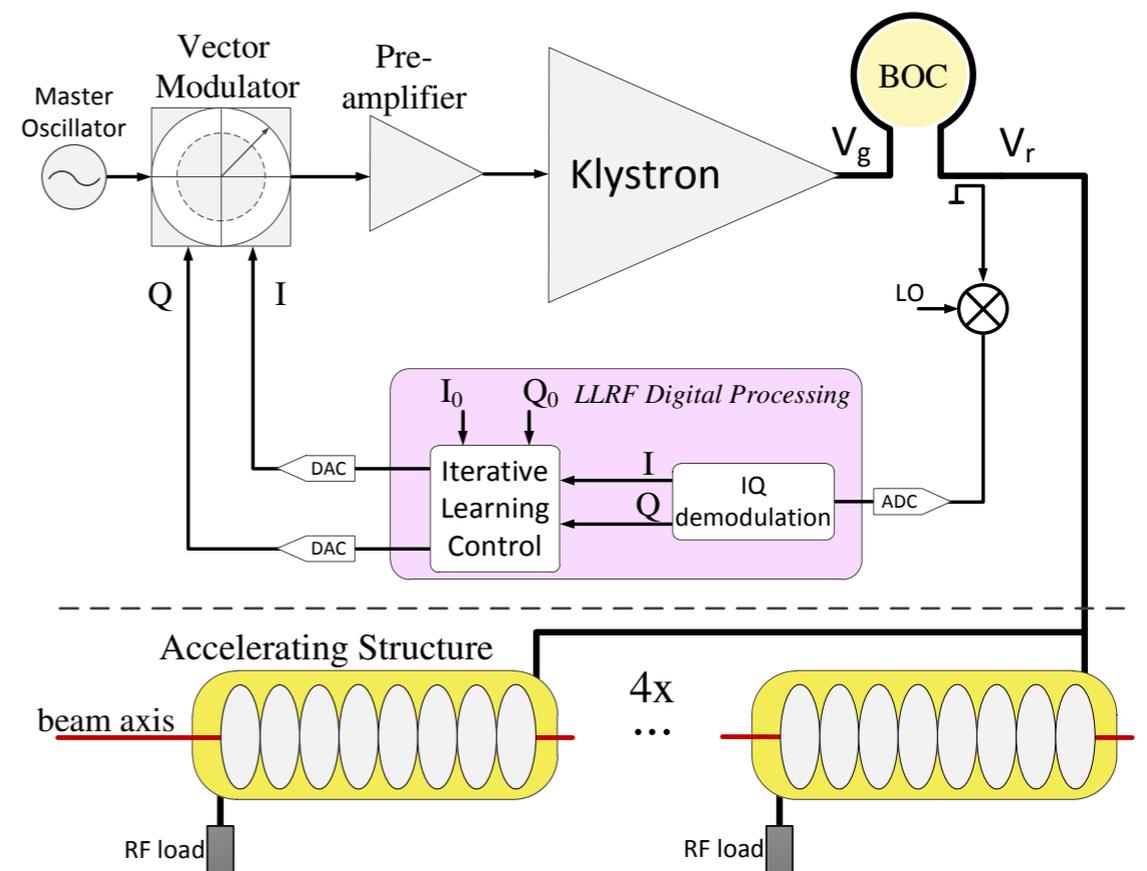


Figure 1: The simplified RF layout of a C-band RF station in the SwissFEL beamline.

Finding the transfer function for the system

Relationship between klystron output voltage and compressor cavity voltage is:

$$\alpha V_g = V_c(1 + j\tau\Delta\omega) + \tau\dot{V}_c,$$

Where α is related to the cavity coupling coefficient, τ is the filling time of the pulse compressor.

The reflected wave from the pulse compressor is given by:

$$V_r = V_c - V_g$$

Discretize the first equation and do the Z-transform (sort of a discrete Fourier transform), and you can find the transfer function for the cavity:

$$G_{BOC}(z) = \frac{V_r(z)}{V_g(z)} = \frac{T_s(\alpha - 1) - \tau - jT_s\tau\Delta\omega + \tau z^{-1}}{T_s + \tau + jT_s\tau\Delta\omega - \tau z^{-1}}$$

RF drive (modulator, pre-amplifier, and klystron) are modeled as a 1st-order low pass system. So, overall transfer function from DAC inputs to cavity output is:

$$G(z) = K \frac{1 - \gamma}{1 - \gamma z^{-1}} G_{BOC}(z).$$

I and Q representation

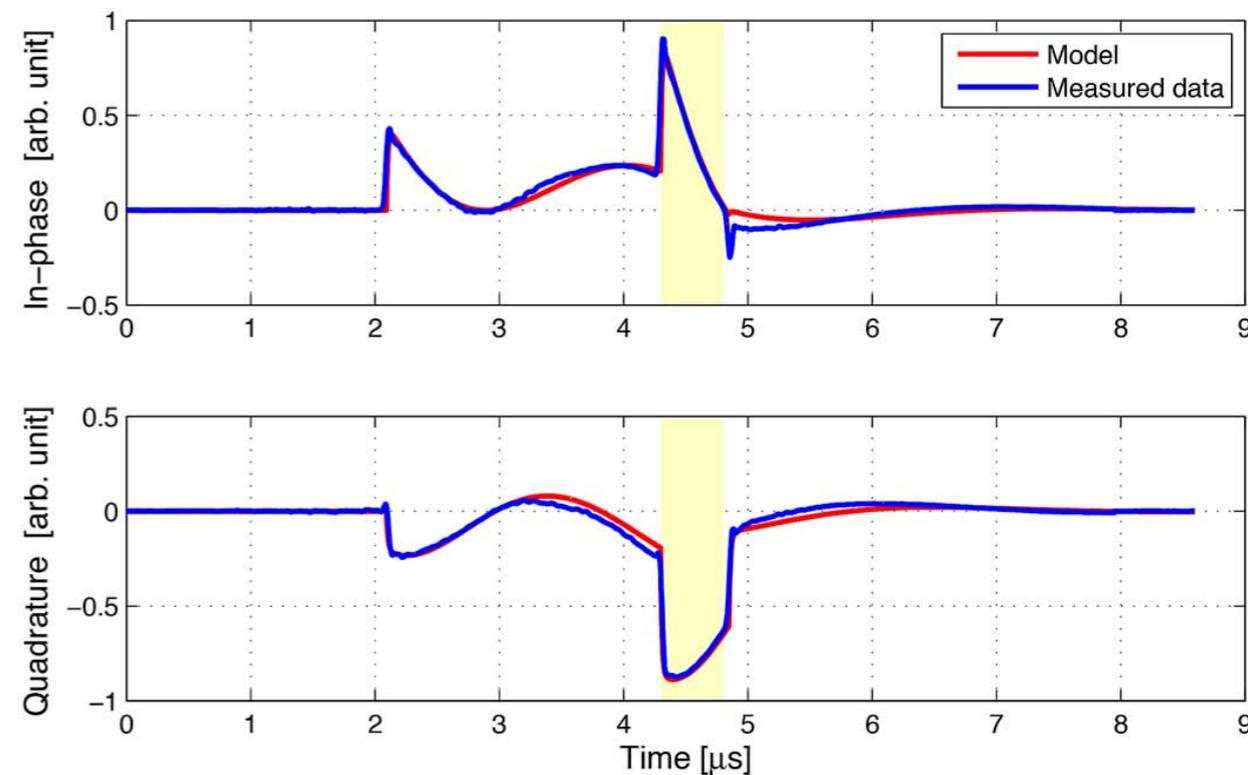
Using “lifted system representation” the equations can be written in an I and Q representation:

$$y_I + jy_Q = G_{IQ} (u_I + ju_Q)$$

where G_{IQ} is a $N \times N$ “lower-triangular Toeplitz matrix of the impulse response $h(k)$ ” derived from the transfer function.

G_{IQ} is then split into real and imaginary parts G_r and G_i such that $G_{IQ} = G_r + jG_i$:

$$y_I = G_r u_I - G_i u_Q$$
$$y_Q = G_i u_I + G_r u_Q.$$



Comparison of the model's predicted output vs. measured I and Q waveforms.

Cost Function

Stacking the I and Q terms, you get the following expression for the relationship between input and output signals:

$$y = Gu + d, \quad y, u \in \mathbb{R}^{2N}, \quad G \in \mathbb{R}^{2N \times 2N}$$

Where d is the output disturbance, which captures the uncertainty about the system. The algorithm will make several iterations. Measured output at an iteration ‘ i ’ is:

$$y_i = Gu_i + d$$

The optimization algorithm calculates the input for the next iteration (u_{i+1}) as the solution of an optimization problem that minimizes the following cost function:

$$J_{i+1}(u_{i+1}) = \|y_d - y_{i+1}\|_X^2 + \|u_{i+1} - u_i\|_R^2$$

X and R are positive $N \times N$ diagonal matrices. How are they determined?

Calculating the Optimal Input

The disturbance term can be estimated from the current iteration:

$$d \simeq y_i - Gu_i$$

Which you can plug into the cost function to give:

$$\begin{aligned} \tilde{J}_{i+1}(u_{i+1}) = & u_{i+1}^T (R + G^T X G) u_{i+1} \\ & - 2 \left(u_i^T R + (y_d - y_i + Gu_i)^T X G \right) u_{i+1} \end{aligned}$$

From which the optimal input for the next iteration can be calculated:

$$u_{i+1} = u_i + (R + G^T X G)^{-1} G^T X (y_d - y_i), \forall i \geq 0$$

Finally, The Algorithm

1: **Initialize** Phase jump regime: constant amplitude, phase jump of 180°

2: **Do**

3: Measure the output I and Q waveforms

4: Compare to the reference trajectories, $e_i = y_d - y_i$.

5: Update the input waveforms

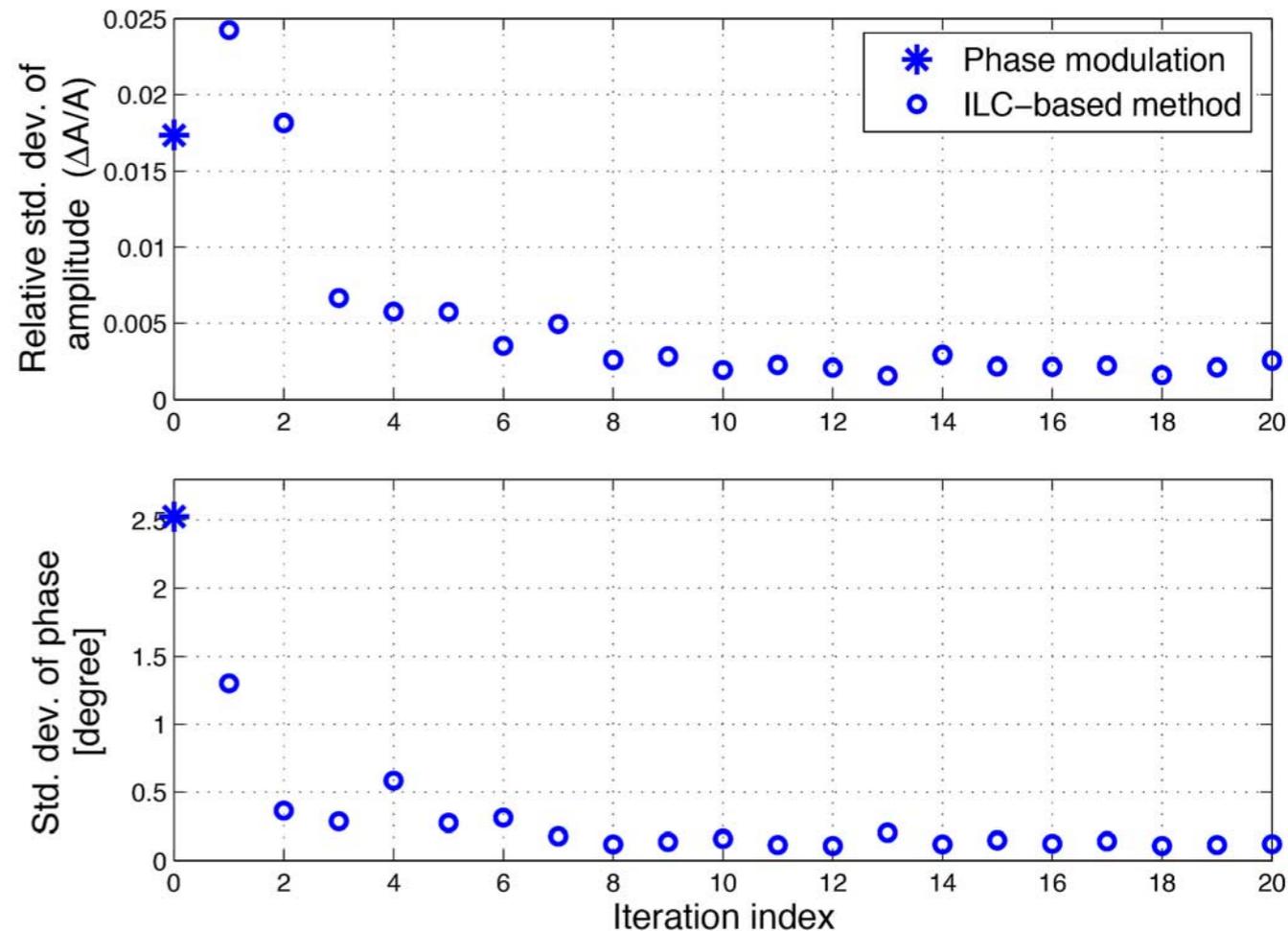
$$u_{i+1} = u_i + (R + G^T X G)^{-1} G^T X e_i \forall i \geq 0.$$

6: Check the limits $u_{\text{low}} \leq u_{i+1} \leq u_{\text{up}}$

7: **If** Convergence achieved

8: **Stop**

9: **Repeat**

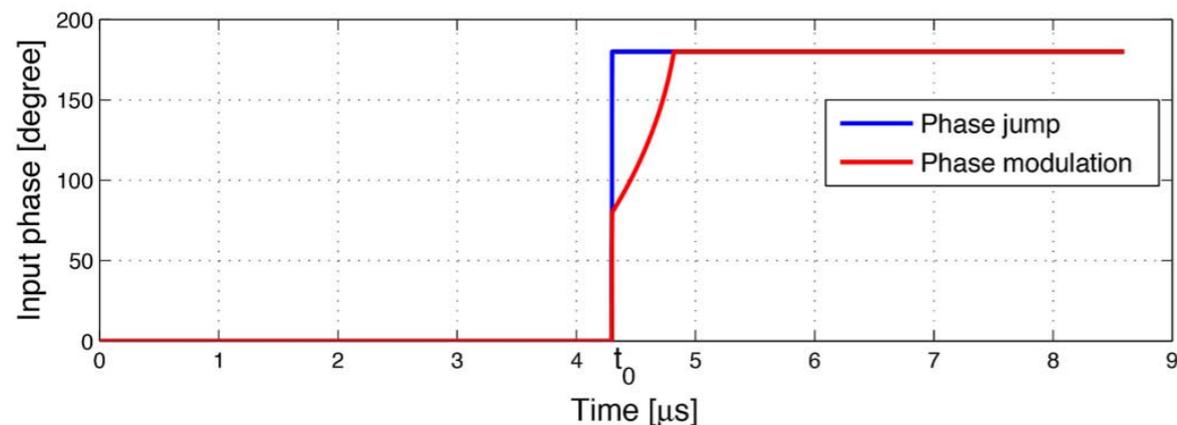
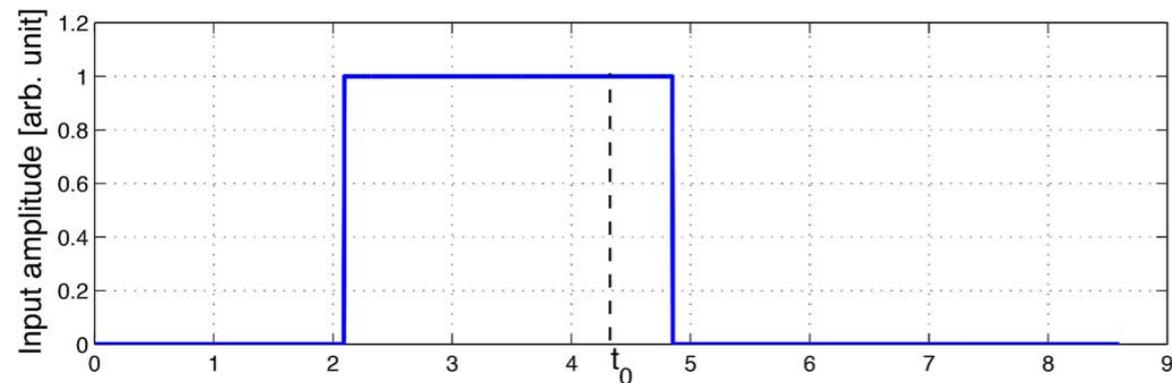


For each iteration, I and Q is measured over ten beam pulses, to suppress noise. After the input waveform is updated, the algorithm pauses for a while to let the cavity temperature re-equilibrate.

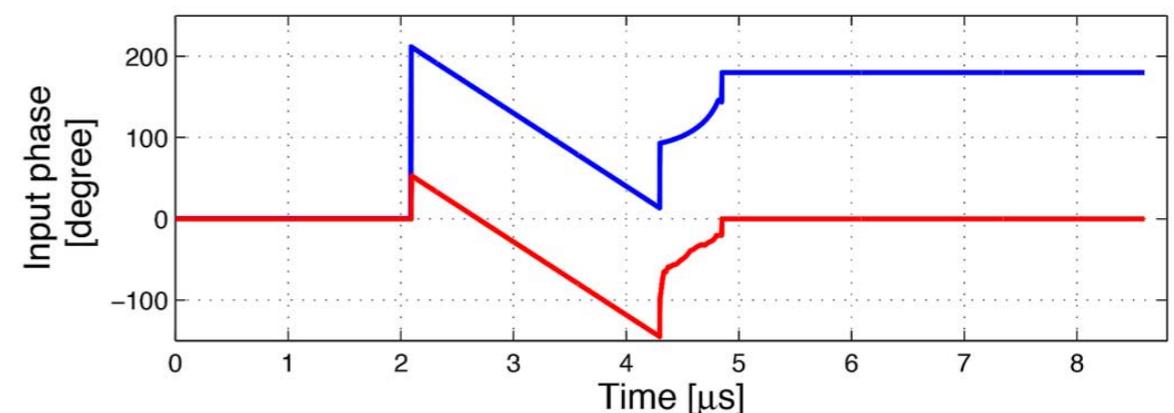
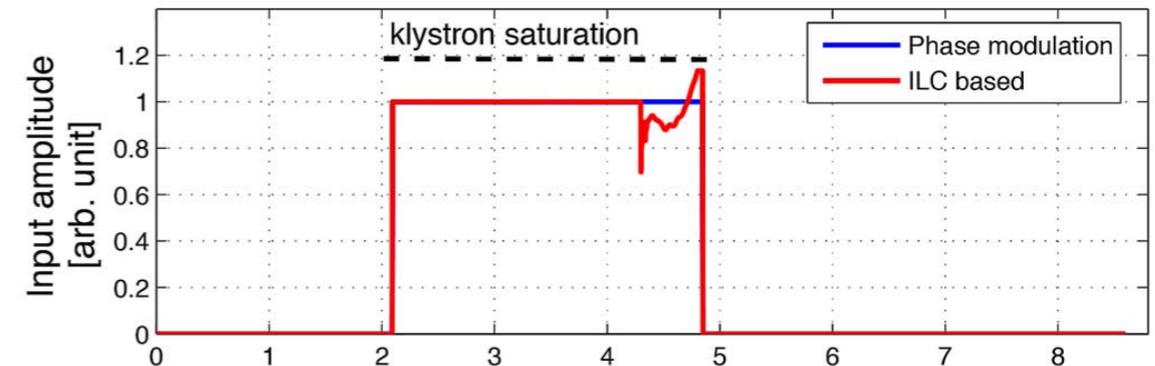
Klystron Input Waveform Before and After Optimization

'Phase jump' waveforms are used as a starting point for the algorithm.

Before



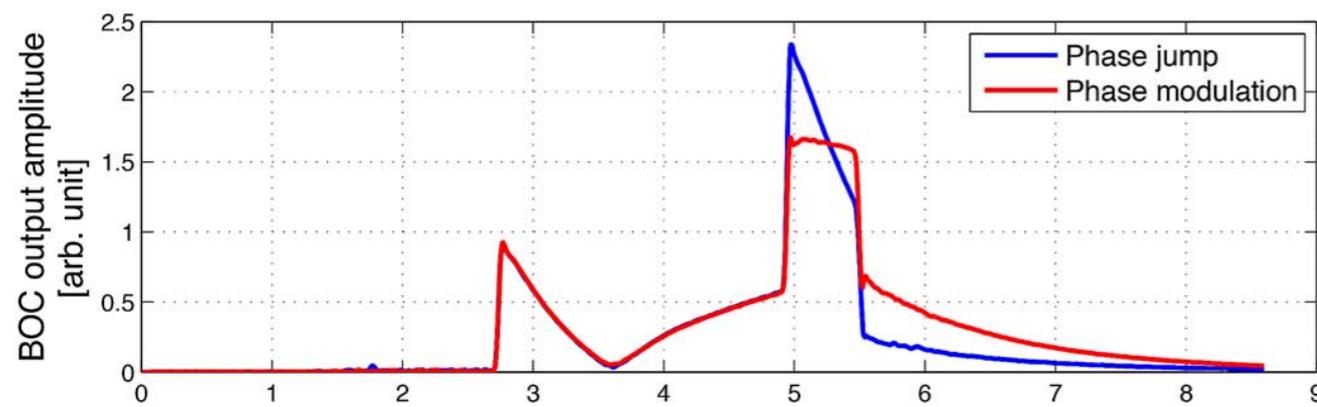
After



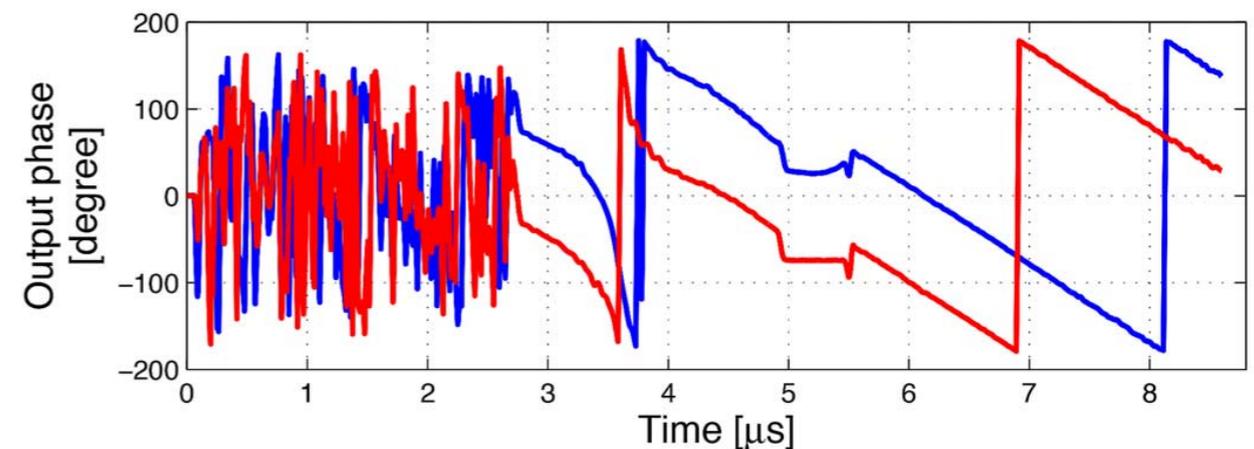
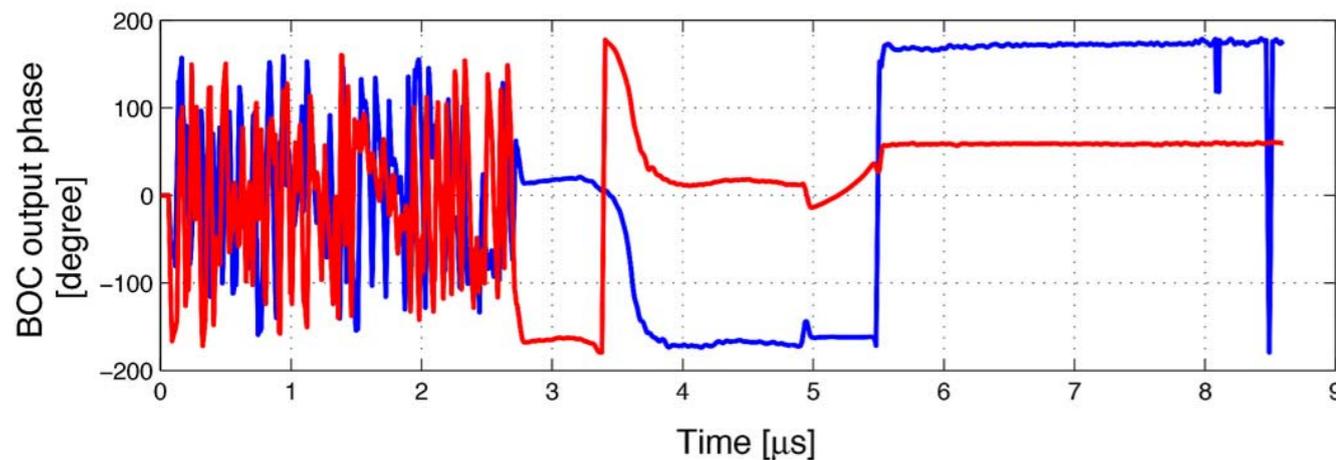
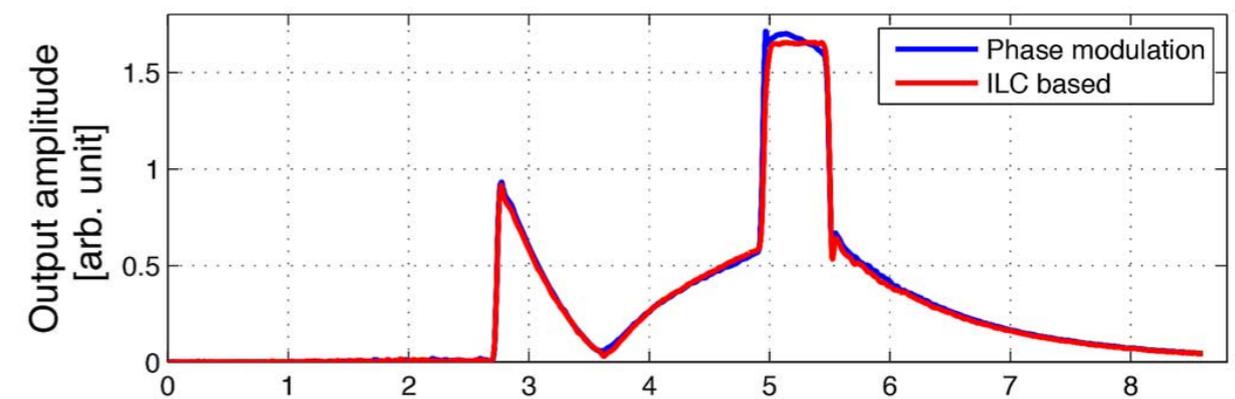
(Phase modulation is an alternative scheme mentioned in the paper, where the phase waveform is analytically determined in advance, and programmed into the modulator. It is shown for comparison to the ILC approach.)

Cavity Output Waveforms After Optimization

Before



After



(Compare 'phase jump' before to 'ILC based' after)

Remarks and Questions

- Authors report losing about 20% of the potential energy gain by using this flattening scheme, which is a pretty steep cost.
- “10 output waveforms are captured and filtered to suppress both random noise as well as the repetitive non-IQ demodulation patterns.” What are the details of this filtering? Just averaging?
- Not much discussion of the stability of this system, besides “the delay must be precisely measured, otherwise the algorithm may run into instability”. With fancy digital control, how easy is it to determine the stability conditions? Is it even possible?
- The algorithm seems to be something that runs until it converges, and then it stops. How often does it need to run? Will drifting environmental conditions for klystron and cavity invalidate the learned pulse shape?

Extensions

- They use reference I and Q waveforms which give a flat phase and amplitude. How well will this scheme work for arbitrary phase and amplitude waveforms? Could you create custom waveforms with finely-tuned bunch energy and/or phase differences? (You'd still have some issues with bunch energies not being matched to the lattice, so there are some external limits to how far you can go.)